

# **Challenges in Conducting Nonresponse Bias Analyses for Business Surveys: A Perspective from the U.S. Census Bureau**

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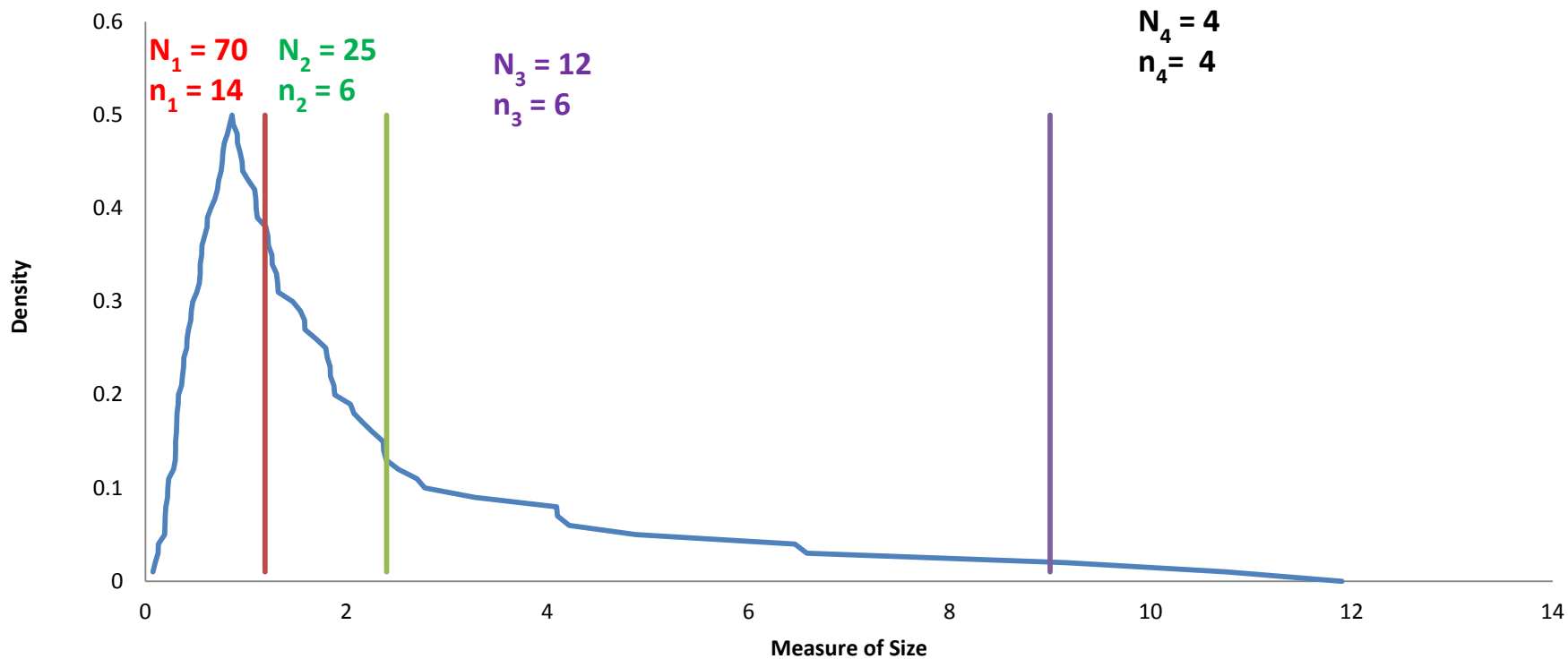
Office of Statistical Methods and Research for Economic Programs

*Presented at the Fourth International Conference on Establishment Surveys*

*Invited Overview Lectures – Session 6*

# SET THE SCENE

# Fictional Stratified Business Population



# Underlying Assumptions

Stratum Number	Population Units ( $N_h$ )	Sampled Units ( $n_h$ )	Stratum Parameters
1	70	14	$\mu_1, \sigma_1$
2	25	6	$\mu_2, \sigma_2$
3	12	6	$\mu_3, \sigma_3$
4	4	4	$\mu_4, \mu_5, \mu_6, \mu_7$

- $\mu_1 \neq \mu_2 \neq \mu_3 \neq \{\mu_4, \mu_5, \mu_6, \mu_7\}$  (or why stratify???)
- The “certainty” units in stratum 4 are unique
  - Self-representing
  - There aren’t very many “large” units in the population
- The **auxiliary variable** used for stratification variable is positively correlated with the survey characteristic(s) of interest

# Design Stage

Population Units ( $N_h$ )	Sampled Units ( $n_h$ )	Stratum Parameters	Sampling Rate $n_h/N_h$	Design Weight
70	14	$\mu_1, \sigma_1$	$14/70 = 0.2$	$70/14 = 5$
25	6	$\mu_2, \sigma_2$	$6/25 = 0.24$	$25/6 = 4.17$
12	6	$\mu_3, \sigma_3$	$6/12 = 0.50$	$12/6 = 2$
4	4	$\mu_4, \mu_5, \mu_6, \mu_7$	$4/4 = 1.00$	$4/4 = 1$

# “Reality”/Challenges

Population Units ( $N_h$ )	Sampled Units ( $n_h$ )	Respondent Units ( $r_h$ )	Sampling Rate $n_h/N_h$	Response Rate $r_h/n_h$
70	14	7	$14/70 = 0.2$	$7/14 = 50\%$
25	6	3	$6/25 = 0.24$	$3/6 = 50\%$
12	6	6	$6/12 = 0.50$	$6/6 = 100\%$
4	4	3	$4/4 = 1.00$	$3/4 = 75\%$

- Larger units very different from smaller units
- Larger units more likely to respond than smaller units
- “Representative” subsample?

# In General

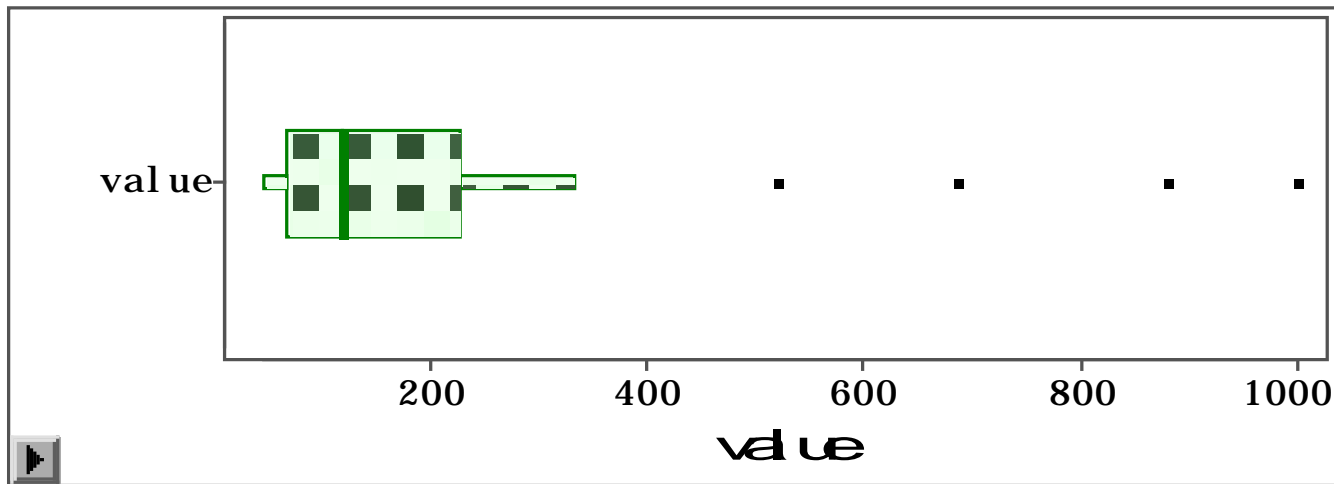
- Business populations are positively skewed
- Business data may not be positively skewed
  - Sales, Payroll, Employment
    - Positively skewed, non-negative by definition
  - Income
    - Real valued (bell shaped curve)
- Estimates of interest – generally TOTALS

# Not All Units Are “Equal”

- Unit response rate
  - Unweighted proportion of responding units
  - One per program/survey
- Total Quantity Response Rate
  - weighted proportion of an estimate reported by responding units and from equivalent quality sources
  - 1 rate per key item/program (can be **several**)

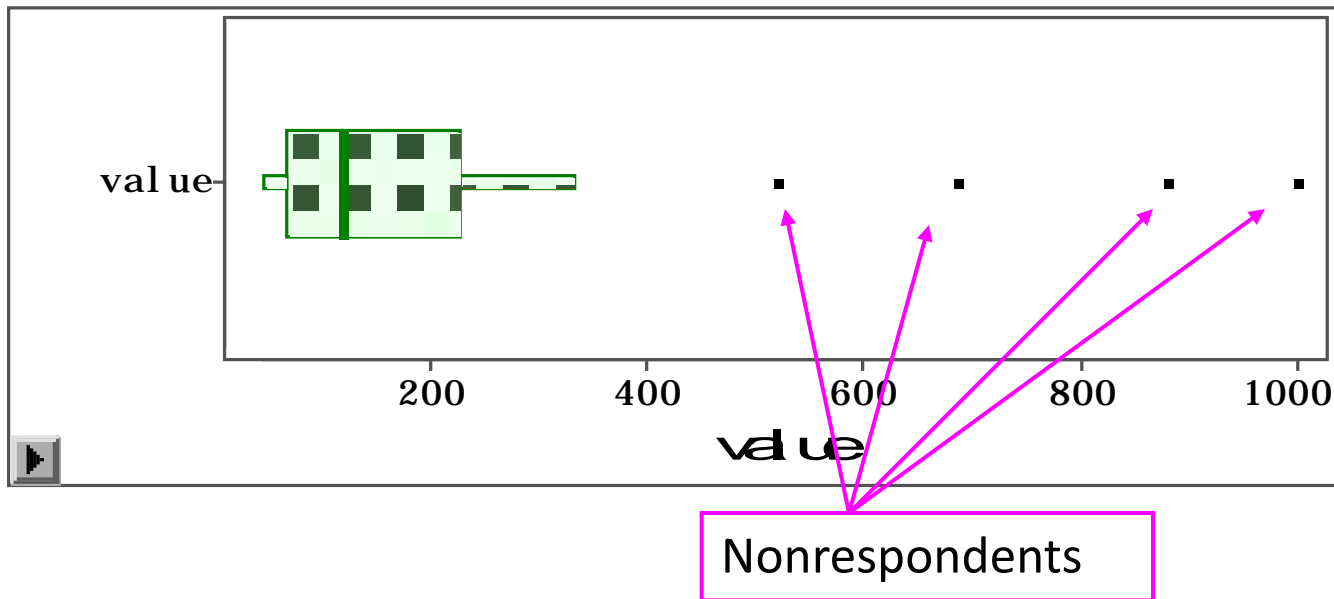


# Return to Fictional Example



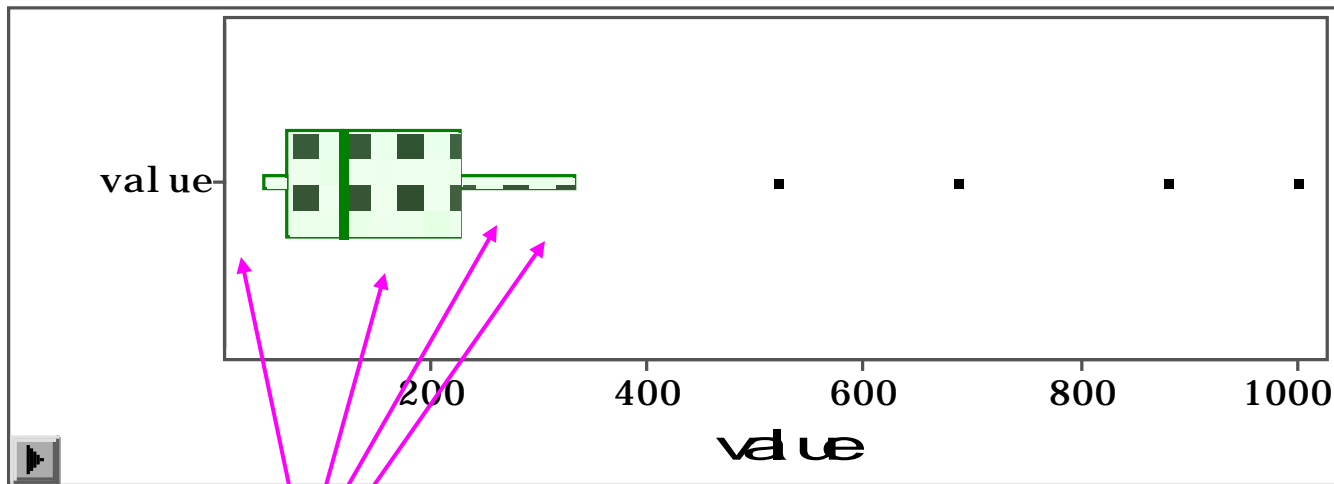
- Skewed business population
- 30 sampled units
- 4 units provide  $\approx 47\%$  of TOTAL Value
  - Certainty units (census)
  - Noncertainty units (sampled)

# Not All Units Are “Equal”



- Unit response rate =  $26/30 \approx 87\%$
- Total Quantity Response Rate (Value) =  $3423/6507 \approx 53\%$

# Not All Units Are Equal



Nonrespondents

- Unit response rate =  $26/30 \approx 87\%$
- Total Quantity Response Rate (Value) =  $6023/6507 \approx 93\%$

# Types of Units

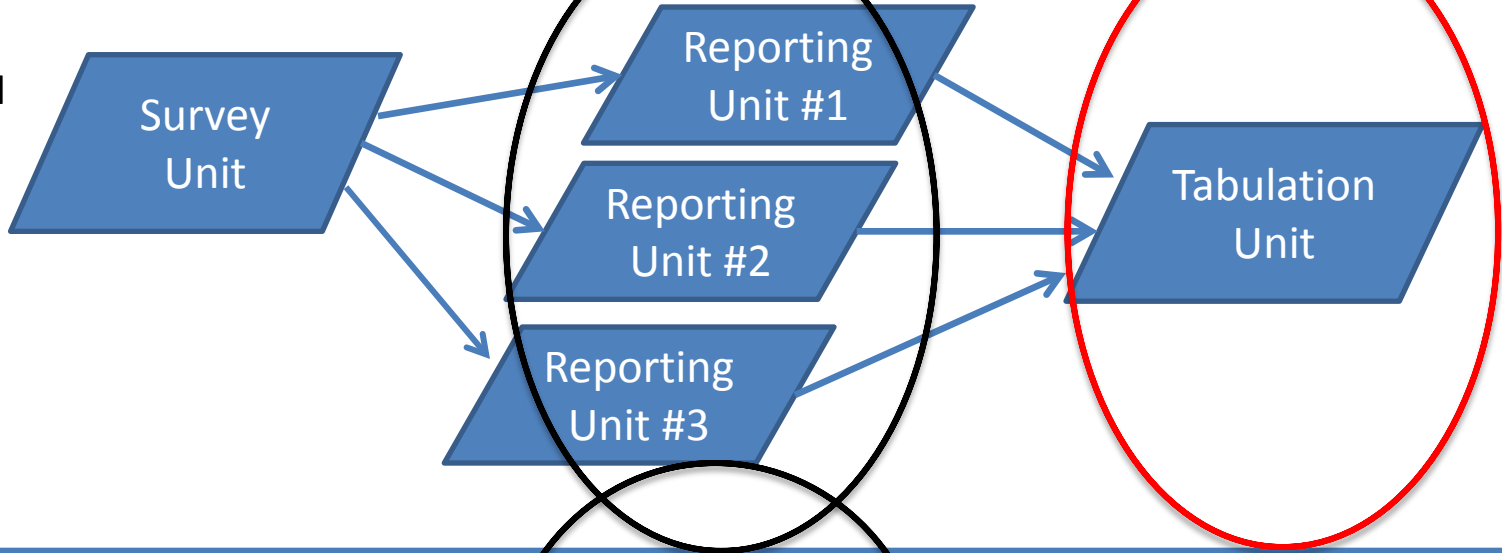
Type of Unit	Definition	Established By
Survey Unit	An entity selected from the underlying statistical population of similarly-constructed units	Frame
Reporting Unit	An entity from which data are collected	Sampled unit(s) providing the data
Tabulation Unit	An entity that houses the data used for estimation/tabulation	Program managers and/or methodologists

## Simplest Case

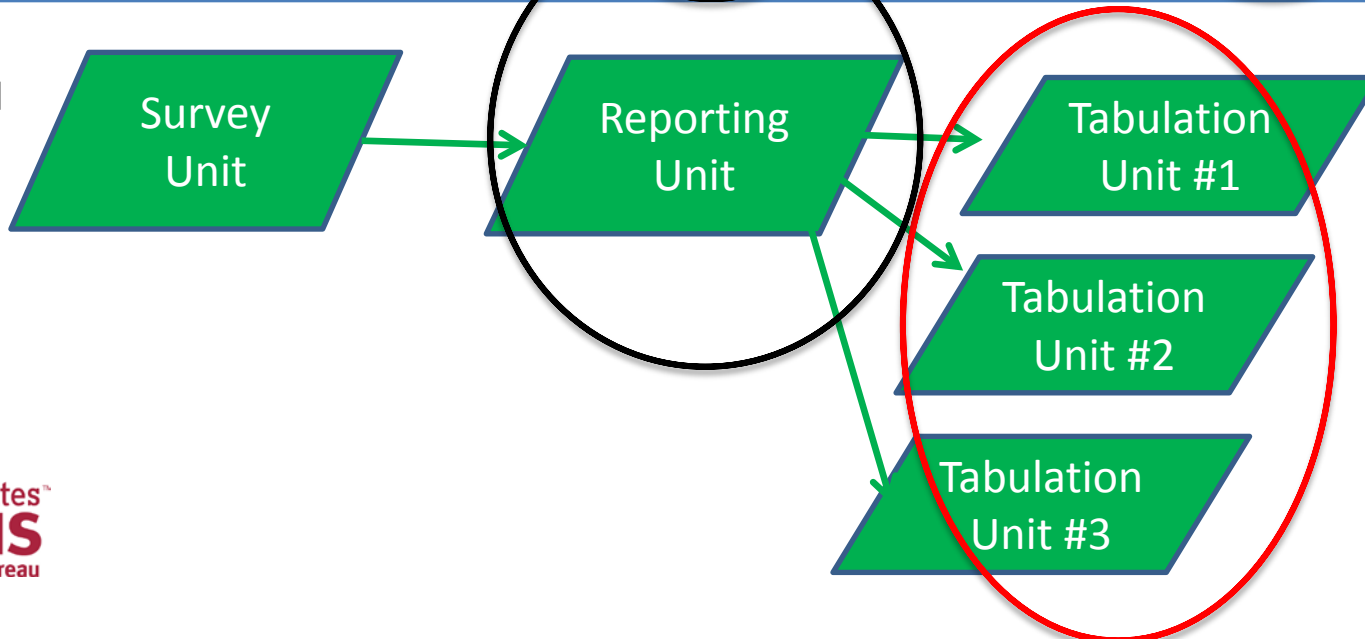


# Types of Units (Equally Realistic)

At statistical period  $t$





At statistical period  $t$



# One More Challenge

Provide the number of employees working at this establishment on March 15, 2011

Category		Value
1a. Production workers	 <b>Detail items</b>	<To Be Collected>
1b. Other employees		""
1c. Total workers	 <b>Total item</b>	""

- Total items collected from each respondent
  - Administrative data may be available for some units
- Detail items
  - Depend on category (industry)
  - May not be available from respondent

Getting More Formal

# **NONRESPONSE BIAS ANALYSIS CONSIDERATIONS**

# The Issues

- Administrative Standards/Requirements
- Statistical Issues
  - Data quality
  - Representatives of respondent set
    - Response mechanism
    - Mitigation strategies
      - Behavioral protocols
      - Statistical adjustments
  - Impact of nonresponse bias on estimates



# Nonresponse Bias (Total)

SAMPLE ( $n$  units)

$$\hat{Y} = N\bar{y}_n = N\left(\sum_{i=1}^n y_i / n\right)$$

RESPONDENTS ( $r$  units)

$$\hat{Y}_r = N\left(\sum_{i=1}^r y_i\right) = \frac{N}{n}(r\bar{y}_r)$$

Observed (respondent data)

NONRESPONDENTS ( $nr$  units)

$$\hat{Y}_{nr} = N\left(\sum_{i=r+1}^n y_i\right) = \frac{N}{n}(nr(\bar{y}_{nr}))$$

Not observed (nonrespondent data)

# Some (Simplified) Formulae

- Bias of unadjusted total (respondent data)

$$\begin{aligned} B &= N(\bar{y}_r) - N(\bar{y}_n) \\ &= N \left\{ (\bar{y}_r) - \left[ \left( \frac{r}{n} \right) (\bar{y}_r) + \left( \frac{nr}{n} \right) (\bar{y}_{nr}) \right] \right\} \\ &= N \left\{ \frac{nr}{n} (\bar{y}_r - \bar{y}_{nr}) \right\} \end{aligned}$$

- Unbiased if
  - Complete response
  - Mean value per respondent = mean value per nonrespondent  $\Rightarrow$   
Items may be affected by nonresponse bias differently

# Stochastic View

$$E(\bar{y}_r - \bar{y}_n) = \frac{\sigma_{yp}}{\bar{p}}$$

Where  $\sigma_{yp}$  is the covariance between the survey variable,  $y$ , and the response propensity,  $p$

- What mechanisms produce the covariance?

Source: Tucker, Dixon, and Cantor (2007). Measuring the Effects of Unit Nonresponse in Establishment Surveys. Third Conference on Establishment Surveys (ICES III)

**ARE YOU READY TO CONDUCT A  
NONRESPONSE BIAS ANALYSIS?**

# The “Structured” Detective Work

1. Determine the potential for nonresponse bias
2. Examine the extent of nonresponse bias
3. Understand the response mechanism
4. Mitigate the nonresponse bias

Repeat, repeat, repeat...

Administrative requirements...

# **DETERMINE THE POTENTIAL FOR NONRESPONSE BIAS**

# In Case You Weren't Listening to Brian

## OMB Standard 1.3 (Survey Response Rates)

- Agencies must design the survey to achieve the highest practical rates of **response...to ensure that survey results are representative of the target population** so that they can be used with confidence to inform decisions.
- ***Nonresponse bias analyses must be conducted if unit or item response rates suggest the potential for bias to occur.***

# More Definitions and Concepts

- Respondent
- Reported Data
- Equivalent Quality, but Not Reported Data
- Required Data Items



# What is a Respondent?

A respondent is an *eligible* unit for which

- an attempt was made to collect data;
- the unit belongs to the target population;
- the unit provided *sufficient data* to be classified as a response.

[Source: Census Bureau Standard: Response Rate Definitions, Version 1.0.]

# Reported Vs. Equivalent Quality

- **Reported Data** are directly received from the **reporting unit** for the survey questionnaire in the data collection period.
- **Equivalent Quality (but Not Reported) Data** are indirectly received from the **reporting unit or the tabulation unit** in the data collection period

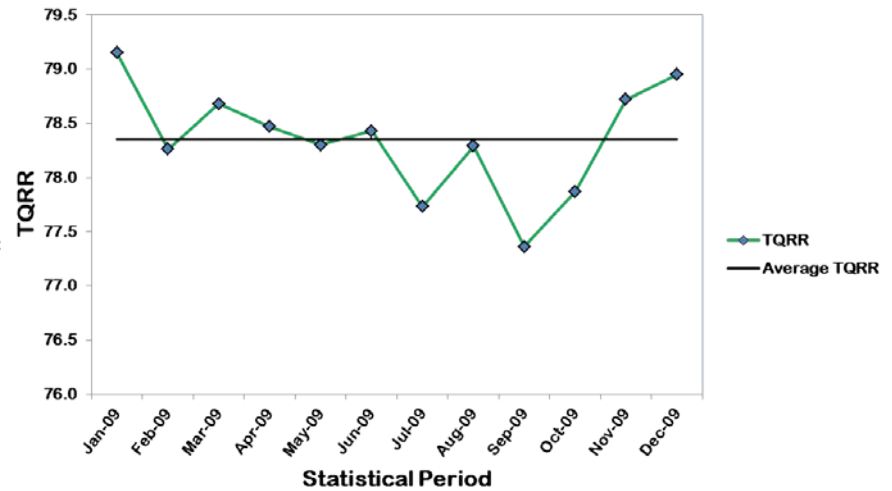
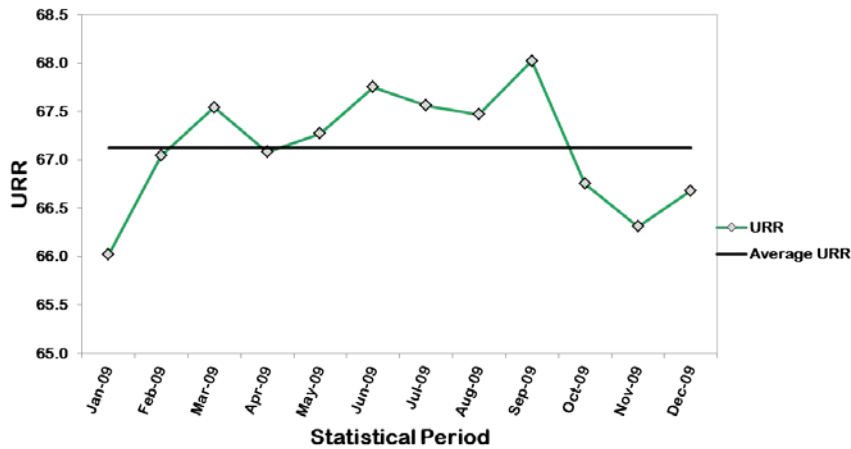
# Response Rates (Refresher)

- **Unit Response Rate (URR)** – the rate of the total unweighted number of “responding” units to the total number of sampled units eligible for tabulation.
  - 1 rate per program
- **Total Quantity Response Rate (TQRR)** – the weighted proportion of a key estimate reported by responding units and from equivalent quality sources.
  - 1 rate per key item/program (can be **several**)

# Response Rate Analyses

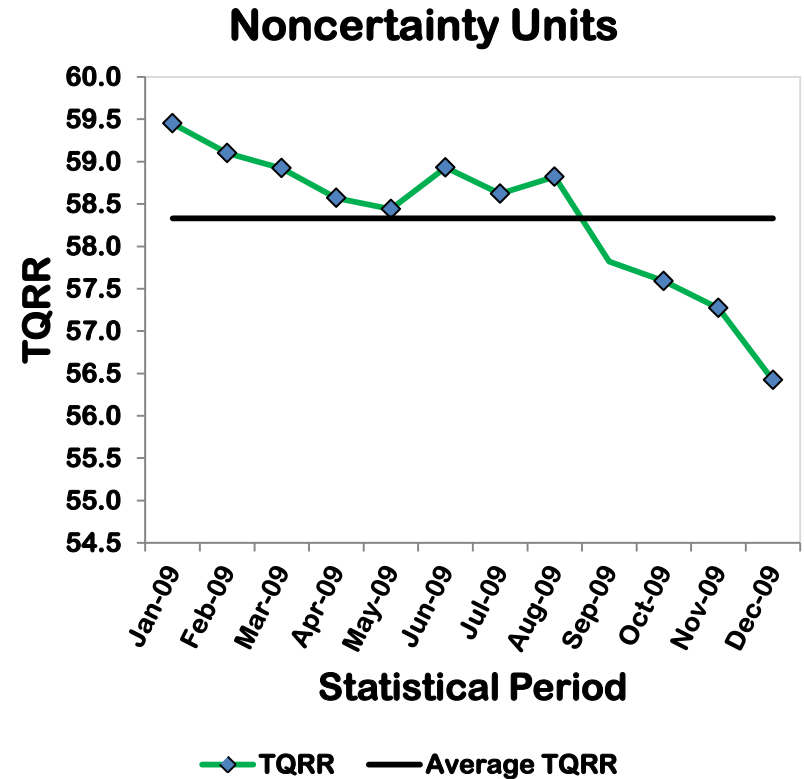
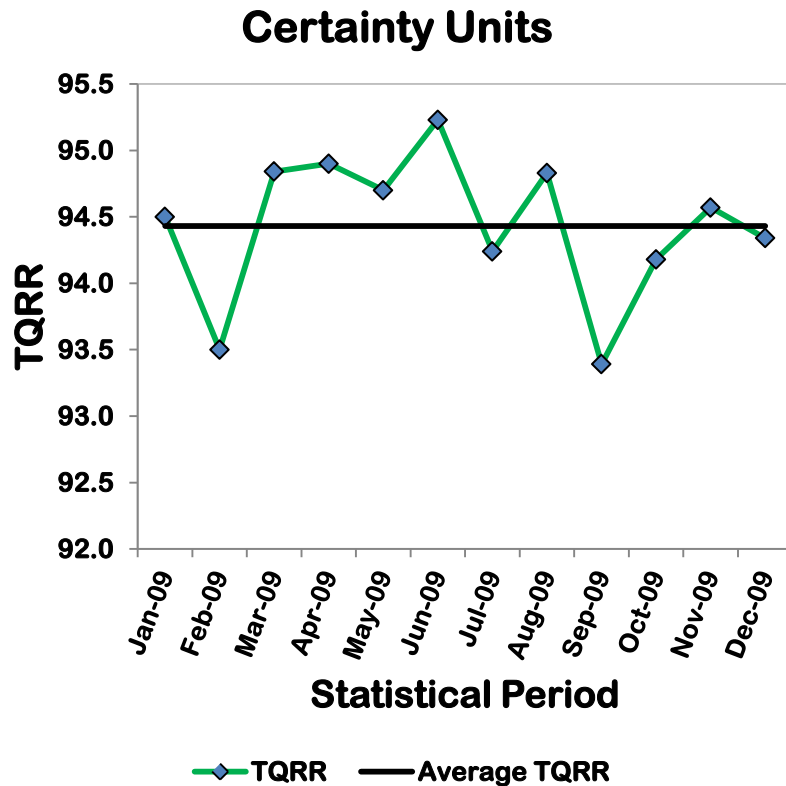
- Compute the rates
  - For program
  - Different (meaningful) subgroups
    - Sector/Industry
    - Certainty/Noncertainty status
- Analyze the rates
- *Monitor the rates over time*

# URR and TQRR (Sales)



Source: Monthly Retail Trade Survey

# TQRR for Sales: By Certainty and Noncertainty Status



Response Rates as Process Control Measures

# **DIGRESSION #1**

# Response Rates as Quality Measures

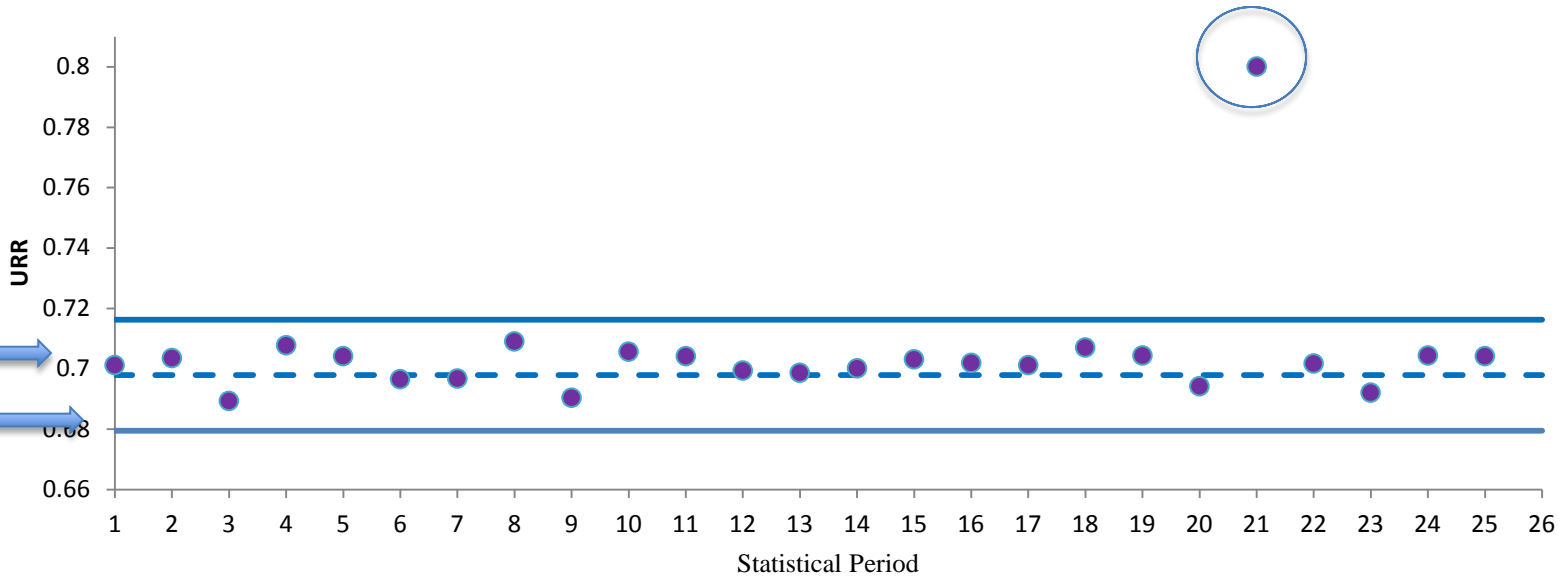
- Assess the state of the process
- Understand the response rate process capability
- Monitor over time

González, Y. and Oliver, B. (2012). Producing Control Charts to Monitor Response Rates for Business Surveys in the Economic Directorate of the U.S. Census Bureau. FCSM Research Conference.

Thompson, Katherine J. and Oliver, B. (2012). Response Rates in Business Surveys: Going Beyond the Usual Performance Measure . Journal of Official Statistics.



# P-chart for URR (Fictional Series)



- Time-series plot of URR
- Centerline (process average)
- Control Limits

Understanding the Response Mechanism

# **DIGRESSION #2**

# Response Mechanisms

- Ignorable
  - Model can “explain” the response mechanism
  - Auxiliary variable (covariate) that “explains” nonresponse is **not** the studied variable(s)
  - Nonresponse can be “ignored” *after the estimates are adjusted with respect to the model*
- Nonignorable
  - Probability of response depends on studied variable (nonresponse systematic, not random)
  - Difficult (if not impossible) to correct through adjustment

# Ignorable Response Mechanism #1: Missing Completely at Random (MCAR)

- Uniform
- Probability of response equal and independent for all units in sample
- Not terribly realistic

# Ignorable Response Mechanism #2: Missing at Random (MAR)

- Probability of response depends on auxiliary variable, not directly related to characteristic(s) of interest
- Probability of response differs by adjustment cell
  - Adjustment cells may or may not be strata
  - Same probability of response for all units in an adjustment cell

# Ignorable Response Mechanism #3: Covariate – Dependent Missing

- Probability of response depends on auxiliary variable, not characteristic(s) of interest (more general formulation)
  - $P(M_i | Y, X) = P(M_i | X)$
- Probability of response differs by unit
- Probability of response **predicted** by level of auxiliary variable

# Options (Ignorable Unit Nonresponse)

- Reweighting
  - Divide sample into weighting cells
  - Increase respondents' weights to represent sample
- Imputation
  - Divide sample into imputation cells
  - Create complete records

# Notation (Reweighting)

Adjustment factor    Adjustment Cell    Sampling weight

$$w_i^{p*} = f_i^p \times w_i$$

$f_i \geq 1$  if  $J_i^p = 1$  (unit  $i$  responded)

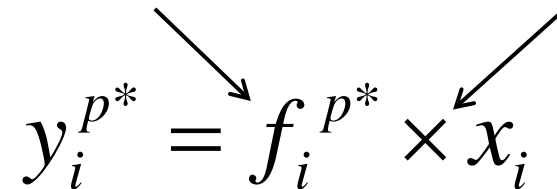
$f_i = 0$  if  $J_i^p = 0$  (unit  $i$  did not respond)

$$\hat{Y}_{adj} = \sum_p \sum_{i \in p} f_i^p J_i^p w_i y_i = \sum_p \sum_{i \in p} w_i^{p*} y_i$$



# Notation (Imputation)

Imputation factor      Auxiliary variable (covariate)

$$y_i^{p*} = f_i^{p*} \times x_i$$


$$\hat{Y}_{imp} = \sum_p \sum_{i \in p} w_i y_i J_i^p + \sum_p \sum_{i \in p} w_i y_i^{p*} (1 - J_i^p)$$

# Reweighting (Mitigation Strategy 1)

## Advantages

- Statistically valid if response model is correct
- Easy to correctly compute variance estimates of totals
- Preserves multivariate relationships between items

## Disadvantages

- Can increase the variance
- Not valid if response set is not a representative random sample

# Imputation (Mitigation Strategy 2)

## Advantages

- Can develop “best” predictive model for each item  $y$
- Can set a hierarchy of imputation methods to attempt in expected order of reliability
- Ratio imputation model parameters can be B.L.U.E.

## Disadvantages

- Predictive model may not be very good
- Does not preserve multivariate relationships
- Difficult to correctly compute variance estimates (especially if composite imputation is used)

# Adjustment Cells

- **Auxiliary variables** (categorical)
  - Available data for all sampled units
  - “Sufficient” respondents in each category
  - May be recoded continuous variables
- Hope
  - Auxiliary variable is correlated with response propensity; **and**
  - Auxiliary variable is correlated with outcome

# Adjustment Effects on Mean or Totals

Auxiliary Variable Association with Response (Propensity)	Auxiliary Variable Association with Outcome (Prediction)	
	Low	High
	Low	Bias:-- Variance:--
High	Bias:-- Variance: ↑	Bias: ↓ Variance: ↓

Little, R.J. and Vartivarian, S. (2005). Does Weighting for Nonresponse Increase The Variability of Survey Means? *Survey Methodology*, **31**, pp. 161-168.

# Certainty Units

Proposition: Nonresponding certainty units always cause some nonresponse bias

- Unique quality → guaranteed inclusion in sample
- Nonignorable nonresponse

# At Last...the Promised Topic

- This talk is titled “Challenges in Conducting Nonresponse Bias Analyses for Business Surveys: **A** Perspective from the U.S. Census Bureau”
- Insights into “tried and true” (aka) methods
  - Cites older analyses (before 2010)
  - Nothing “cutting edge”

Studying internal variation within the data collection

# **COMPARE RESPONDENTS AND NONRESPONDENTS ON FRAME VARIABLES**



# Adjustment Effects on Mean or Totals

Auxiliary Variable(s) Association with Response (Propensity)	Auxiliary Variable Association with Outcome (Prediction)	
	Low	High
	Low	Bias:-- Variance:--
High	Bias:-- Variance: ↑	Bias: ↓ Variance: ↓



# Response Propensity Analysis

- Are categorical variables used to form adjustment cells predictive of unit nonresponse?
  - Logistic regression analysis
- Could other variable be used to form adjustment cells?
- Do response propensities differ between cells?
  - Assess by comparing unit response rates

# Are Categorical Variables Used To Form Adjustment Cells Predictive Of Nonresponse?

Model: 
$$\log\left(\frac{P(I_i^p = 1)}{1 - P(I_i^p = 1)}\right) = \beta^p X_i^p + \varepsilon_i^p$$

Test: 
$$H_0 : \beta^p = 0$$
$$H_A : \beta^p \neq 0$$

# Logistic Regression Models

- Want to **reject** the null hypothesis
  - Propensity model holds
- Need to account for complex survey design
  - PROC SURVEYLOGISTIC<sup>®</sup>
  - Noncertainty units only
- Minimum cell size requirements (challenge!)
  - Actual sample size
  - Effective sample size

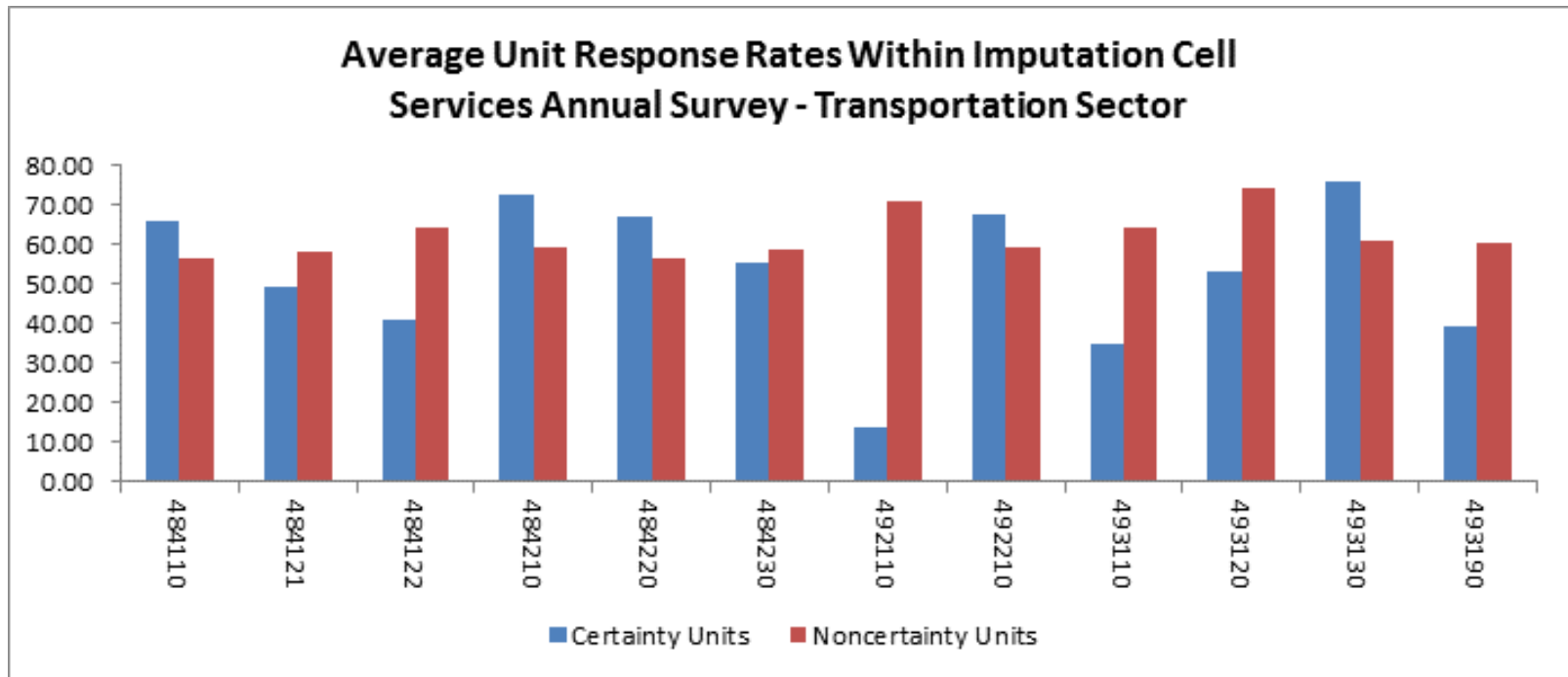
# Annual Capital Expenditures Survey

Percentage of Weighting Cells Where Propensity Model Held					
Size Class Stratum	Survey Year				
	2002	2003	2004	2005	2006
2A	84.1	78.3	84.1	80.3	82.7
2B	78.2	65.6	72.1	73.3	78.8
2C	76.0	52.0	69.0	63.3	70.0
2D	44.7	27.9	34.1	31.5	30.3

Largest companies

Smallest companies

# Do Response Propensities Differ Between and Within Cells?



# Adjustment Effects on Mean or Totals



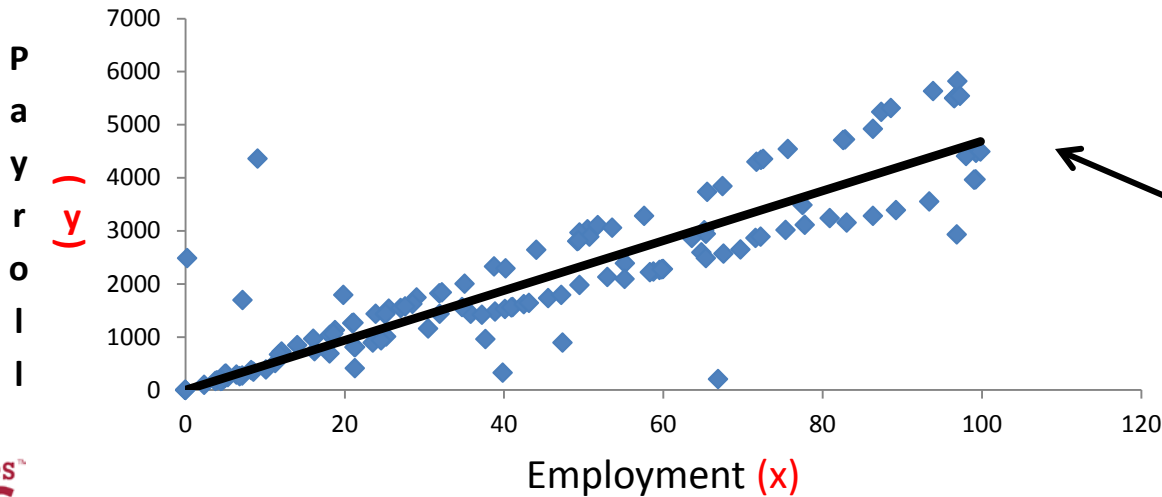
		Auxiliary Variable Association with Outcome (Prediction)	
		Low	High
Auxiliary Variable(s) Association with Response (Propensity)	Low	Bias:-- Variance:--	Bias:-- Variance: ↓
	High	Bias:-- Variance: ↑	Bias: ↓ Variance: ↓

# Response Model Assessment: Prediction Model Evaluation

Model: 
$$Y_i = \beta^p X_i^p + \varepsilon_i^p$$

Test: 
$$H_0 : \beta^p = 0$$

$$H_A : \beta^p \neq 0$$



$$\hat{\beta}^p = \frac{\sum_{i \in p} y_i}{\sum_{i \in p} x_i}$$



# Prediction Model/Regression Analysis

- Want to **reject** the null hypothesis
- WLS linear regression no intercept model

**Trend**  $y_{ti}^* = \beta y_{t-1,i} + \varepsilon_{ti}, \varepsilon_{ti} \sim (0, y_{t-1,i} \sigma^2)$

**Auxiliary**  $y_{ti}^* = \beta x_{ti} + \varepsilon_{ti}, \varepsilon_{ti} \sim (0, x_{ti} \sigma^2)$

- Minimum cell size requirements (challenge!)
  - Actual sample size
  - Effective sample size

# Prediction Model/Regression Analysis

- Need to account for the complex survey design
  - PROC SURVEYREG®
  - Noncertainty units only
- Want model to be highly predictive
  - Model  $R^2$  = measure of “predictive power” of auxiliary variable on item of interest
- Adjustment cell as “instrumental variable”

# Example: ACES

## Percentage of Weighting Cells Where Prediction Model Held

Size Class Stratum	Survey Year				
	2002	2003	2004	2005	2006
2A	93.8	93.1	92.6	93.3	94.8
2B	85.3	89.9	84.1	78.9	88.7
2C	77.0	74.6	73.6	80.8	74.6
2D	56.1	45.9	56.3	52.4	58.7

Largest companies



Smallest companies



# Are the Respondents a Random Subsample Within Adjustment Cell?

- Assessing the assumption of “ignorable” nonresponse
- Need **auxiliary variables** available for all sampled units
  - Proxy variables for characteristic(s) of interest
- Adjustment cells may not be strata
  - Must account for differential sampling

# Are the Respondents a Random Subsample Within Adjustment Cell?

- Are the respondent-based means different from the full-sample means?
- *Are respondents systematically different from nonrespondents?*

# Examining the “Balance”

$$H_0 : \mu_R^p = \mu_n^p$$

$$H_A : \mu_R^p \neq \mu_n^p$$

- Are the respondent-based means different from the full-sample means?
- Measured on **auxiliary variables**

# Examining the “Distance”

$$H_0 : \mu_R^p = \mu_{NR}^p$$

$$H_A : \mu_R^p \neq \mu_{NR}^p$$

- Are respondents systematically different from nonrespondents?
- Measured on **auxiliary variables**

# Examining the “Distance”

$$H_0 : \mu_R^p = \mu_{NR}^p$$

$$H_A : \mu_R^p \neq \mu_{NR}^p$$

- Two-sample t-tests on frame variable
  - Performed within adjustment cell  $p$
  - Cross-sectional and longitudinal analysis

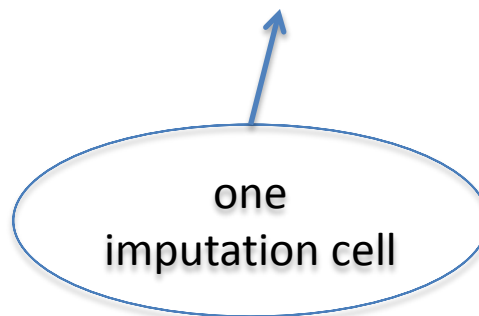


# T-tests


- Want to **fail to reject** the null hypothesis
- Need to account for complex survey design
  - Weighted unbiased estimates
  - Complex survey variances
  - Noncertainty units only
- Need “sufficient” observations in adjustment cell
  - Respondents and Nonrespondents
  - Challenge for
    - “Large” unit strata (few units to begin with)
    - High nonresponse strata (large variances)

# Quarterly Services Survey (QSS)

		2004				2005			
Sector		Q1	Q2	Q3	Q4	Q1	Q2	Q3	Q4
51	<b>Total Imputation Cells</b>	12	12	12	12	12	12	12	12
	<b>Different Means (<math>\mu_R \neq \mu_{NR}</math>)</b>	0	2	1	0	2	1	1	1



# Cross-sectional Analysis




		2004				2005			
Sector		Q1	Q2	Q3	Q4	Q1	Q2	Q3	Q4
51	Total <b>Imputation</b> Cells	12	12	12	12	12	12	12	12
	Different Means( $\mu_R \neq \mu_{NR}$ )	0	2	1	0	2	1	1	1

- Test whether the **number** of cells with different respondent and nonrespondent means is larger than expected
- No evidence of systematic difference in mean receipts

# Longitudinal Analysis

		2004				2005			
Sector		Q1	Q2	Q3	Q4	Q1	Q2	Q3	Q4
51	<b>Total Imputation Cells</b>	12	12	12	12	12	12	12	12
	<b>Different Means(<math>\mu_R \neq \mu_{NR}</math>)</b>	0	2	1	0	2	1	1	1



- Examine the cells with significantly different means across quarters
- Identify cells that exhibit “consistent” differences
  - Imputation cell 512000T (5 of 8 quarters)

# Chi-Squared Tests for Independence

	Respondents	Nonrespondents	
$0 < \text{weight} < P_{33}$	$r_{11}$	$r_{12}$	$r_{1\bullet}$
$P_{33} \leq \text{weight} < P_{66}$	$r_{21}$	$r_{22}$	$r_{2\bullet}$
$P_{66} \leq \text{weight}$	$r_{31}$	$r_{32}$	$r_{3\bullet}$
	$r_{\bullet 1}$	$r_{\bullet 2}$	$r_{\bullet\bullet}$

- PROC SURVEYFREQ<sup>®</sup>
  - Want to **fail to reject** null hypothesis
- Noncertainty units only

# Sensitivity Analysis

- Presented techniques require auxiliary variables
  - Available for all sampled units
  - Correlated with characteristics
- Other options (sensitivity analysis)
  - Quantile regression (Tucker and Dixon, 2007)
  - “Influence” functions – examine contribution of each weighted observation to tabulated total

# **A FEW OTHER APPROACHES: SOME CONSIDERATIONS**

# Comparison to Other Estimates – Benchmarking to Other Programs

- Alternative estimates may or may not be independent
- Definitions between programs may not agree (**caution advised**)
- **Big** assumption that other set of estimates is “superior” to studied program with respect to sampling and/or measurement errors



# Benchmarking Survey Estimates to those from Another Data Source

- Compare linked microdata
  - Same units, other programs
  - Administrative data (where feasible)
  - Same cautions apply with respect to definitions for items
- Compare early and late respondents on key estimates
  - Not studied extensively for business surveys

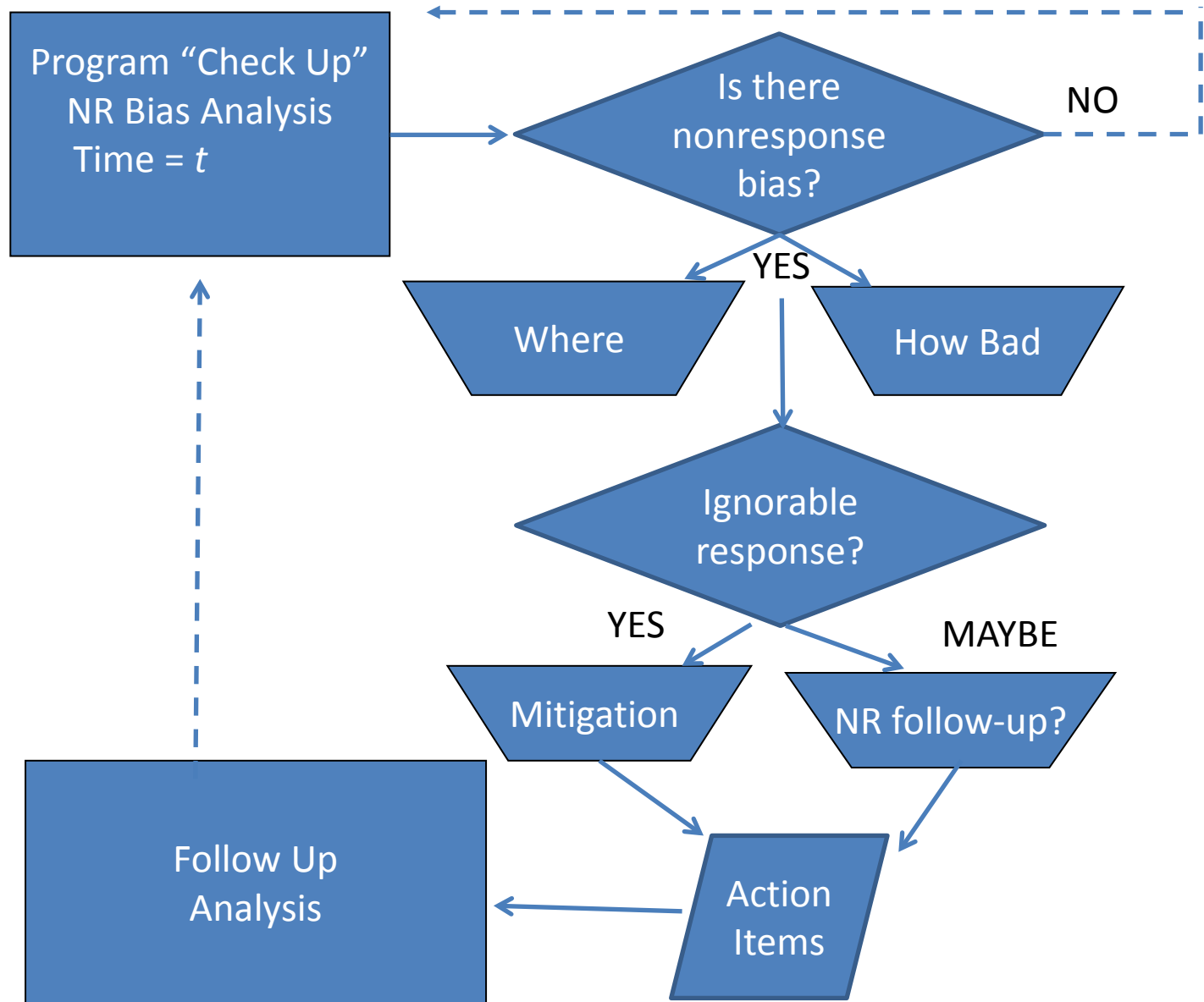
We Did It, Now What?

# **MAKING NONRESPONSE BIAS ANALYSIS EFFECTIVE**

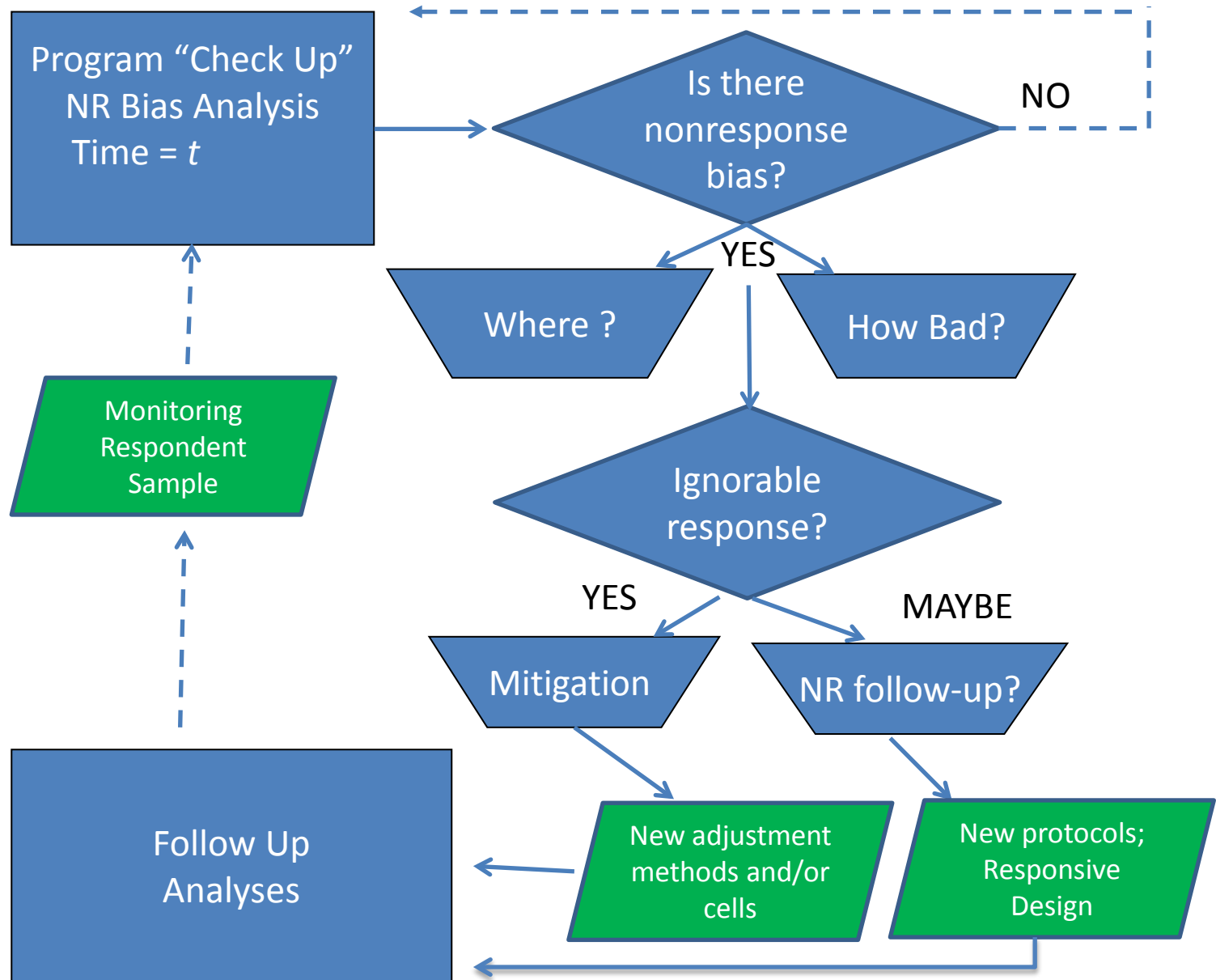
# Official Disclaimer

*The purpose of this presentation is to inform interested parties of research and to encourage discussion of work in progress. Any views expressed are those of the author and not necessarily those of the U.S. Census Bureau.*

# Objectives of NR Bias Analysis



# Useful Outcomes of NR Bias Analysis



# Being Pro-Active

- Monitor respondent sample during collection to avoid nonresponse bias
  - P-charts of unit response rates
  - Contingency table analysis
  - R-indicators
- Especially for nonignorable nonresponse
  - **Study** response contact strategies
    - Qualitative – focus groups, company visits
    - Quantitative – using paradata
  - Responsive designs

# The Beginning...

- **Initial Analysis** (Nonresponse Bias Study)
  - Action items
- **Corrective measures**/process changes
  - Assess over time using the same analysis tools
- **Monitor** stable/in-control process
  - Collaborative effort between methodologists and subject-matter experts

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